1. An internet search finds the claim: "US adult female heights are on average 64.5 inches (5'4 1/2") with a standard deviation of 2.5 inches." The fraction F of such adult females within two standard deviations above the mean value ("average") for a normal distribution is given by the following definite integral

$$F = \int_{64.5}^{69.5} \frac{1}{2.5\sqrt{2\pi}} e^{-\frac{1}{2} \cdot \left(\frac{x - 64.5}{2.5}\right)^2} dx$$

- a) Use Maple to evaluate this exactly and approximate the result to 3 decimal places.
- b) Use the change of variable to the "standard variable" $u = \frac{x 64.5}{2.5}$ to transform this integral to its standard

form in terms of that new variable (which measures the deviation from the average value in multiples of the standard deviation).

- c) Use Maple to evaluate the new integral exactly and approximate it to 3 decimal places.
- d) They should agree. If not find your error.
- e) What percent of this population has a height within two standard deviations above the mean value of 64.5 inches? Answer in a complete English sentence.
- 2. a) Evaluate $\int_0^a x \sqrt{a^2 x^2} dx$ (assuming a > 0) showing all the steps by an appropriate *u*-substitution,

converting the integral entirely to the new variable in this process before evaluating it.

b) Does Maple or your graphing calculator or tech tool confirm your result? Explain.

solution