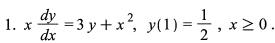
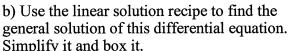
MAT2705-01/02 11F Quiz 3 Print Name (Last, First)

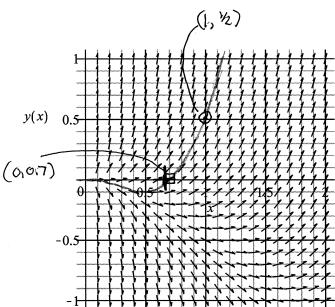
Show all work, including mental steps, in a clearly organized way that speaks for itself. Use proper mathematical notation, identifying expressions by their proper symbols (introducing them if necessary), and use arrows and equal signs when appropriate. Always simplify expressions. BOX final short answers. LABEL parts of problem. Keep answers EXACT (but give decimal approximations for interpretation). Indicate where technology is used and what type (Maple, GC).



a) Hand draw in the solution of this differential equation satisfying the initial condition on the associated direction field to the right. Put a circled dot at the point corresponding to the initial condition. Put a squared dot on the curve where y = 0. Estimate your approximate value of x > 0 where this occurs.



c) Find the solution of this differential equation which satisfies the given initial condition. Simplify it and box it.



d) Solve your solution for the value(s) of x where y = 0 numerically to 2 decimal places and mark the corresponding point on your graph with a cross +. Is this consistent with your part a) result? Explain.

e) Does your initial value problem solution agree with Maple (which might require Expand to multiply out, or Simplify, Simplify to simplify)? If not, can you find your mistake? If so, show the equivalence of your solution wit Maple's.

▶ solution

b)
$$\frac{dy}{dx} = \frac{3}{x}y + x$$

 $x^{3} \left[\frac{dy}{dx} \left(\frac{3}{x} \right) y = x \right]$
 $\left[\frac{-\frac{3}{x}dx}{-\frac{3}{x}} + \frac{-3\ln|x|}{2} \right] = \frac{-3}{x^{2}}$
 $\frac{d}{dx}(yx^{-3}) = xx^{-3} = x^{-2}$
 $yx^{-3} = \int x^{-2}dx = \frac{x^{-1}}{-1} + C$
 $y = x^{3}(-\frac{1}{x} + c) = -x^{2} + Cx^{3}$
 $y = -x^{2} + Cx^{3}$

c)
$$\frac{1}{2} = -1^2 + (.1^3 = C - 1)$$

$$C = \frac{1}{2} + 1 = \frac{3}{2}$$

$$y = \frac{3}{2} \times 3 - \times 2$$

$$d) = 0 \rightarrow (\frac{3}{2} \times -1) \times = 0$$

$$X = 0, \frac{2}{3} \approx 0.67 \iff \text{estimate : 0.7}$$

$$\text{prelty dose, see plot}$$
e) Maple: $y = (-\frac{1}{x} + c) \times 3 = -x^2 + c \times 3$

$$\text{output: } y = (-\frac{1}{x} + c) \times 3 = -x^2 + c \times 3$$

$$\text{expand}$$