MA12/05-02/03 068 Quiz 8 Print Name (Last, First)	
Show all work, including mental steps, in a clearly organized way that speaks for itself. Use proper	r
mathematical notation, identifying expressions by their proper symbols (introducing them if necess	sary), and use
arrows and equal signs when appropriate. Always simplify expressions. BOX final short answers.	LABEL parts
of problem. Keep answers EXACT (but give decimal approximations for interpretation). Indicate v	where
technology is used and what type (Maple, GC). You may use technology to row reduce matrices	and to find
determinants and the (integer) roots of the characteristic equation.	

$$1. A = \left[\begin{array}{rrr} 9 & -4 & 0 \\ -6 & -1 & 0 \\ 6 & 4 & 3 \end{array} \right]$$

- a) Find the eigenvalues and eigenvectors of the matrix A following the full procedure: evaluate the characteristic equation $\det(A-\lambda I)=0$, solve it for the eigenvalues, then backsubstitute each into the linear system of equations whose solution leads to an eigenbasis for the eigenspace associated with that eigenvalue, scaling up your basis vectors so they have integer components. You need to report the characteristic equation, its solutions, and for each eigenvalue the starting augmented matrix and its rref form, from which by hand you must solve for the solution space basis. Label the basis vectors **b1**, **b2**, **b3**.
- b) Finally augment them into a matrix B and use it to solve the linear system By = (1,-2, 3) in order to express the vector x = (1,-2, 3) as an explicit linear combination of the eigenvectors: x = ?b1 + ?b2 + ?b3.

▶ solution