- (i) Using one of the two shorthand notations:  $R_1 \leftrightarrow R_2$   $R_1 \rightarrow 2R_1$   $R_1 \rightarrow -3R_2 + R_1$  reduce the matrix  $\begin{bmatrix} 6.5.4 \\ 1.2.3 \end{bmatrix}$  swapraw (1,2) mulrow (1,2) addrow (2,1,-3) to its fully reduced raw exhelon form (ref) by a series of single row operations, recording each intermediate matrix and the row operation that created it.
- Consider a body that moves horizontally through a medium whose resistance is proportional to the square of the velocity V, so that  $dV/dt = -kv^2$ . Show that  $V(t) = \frac{Vo}{1+V-b+1}$ .
  - 4 OPTIONAL PART only for those students who are sure everything they did above is correct and who have extra time to kill:

    If we choose time units so that  $V(1) = V_1$  is the value of the velocity at time t=1, solve for k and re-express V(t) in terms of  $V_1$ , simplifying your result.