Show all work, including mental steps, in a clearly organized way that speaks for itself. Use proper mathematical notation, identifying expressions by their proper symbols (introducing them if necessary), and use arrows and equal signs when appropriate. Always simplify expressions. BOX final short answers. LABEL parts of problem. Keep answers EXACT (not decimal approximations, if possible).

$$f(x) = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{2n+1} = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \frac{x^9}{9} - \dots$$

- a) Use the ratio test to find the radius R of convergence of this power series (such that the senes converges for IXI < R and diverges for IXI > R).
- b) Check the endpoints of the open interval -R < x < R for convergence in order to state the complete interval of convergence in this same notation. Explain your claims.
- f(1/2) is an alternating series so you can easily estimate the truncation error. Whatis the least number in for which the partial sum Sn up to the nth power term gives the value of f(1/2) to 3 decimal place accuracy? Give Sn to at least of the spect value is $f(1/2) = a_1 + a_2 + a_3 + a_4 + a_4 + a_5 + a_$
- d) The exact value is $f(1/2) = \arctan(1/2)$. What is the value of the remainder f(1/2) Sn for the n you picked in part c)? Is it smaller in absolute value than your estimate in part c)?