

Show absolutely all work (no scratch paper calculations or mental calculations unreported) on this sheet in a clearly organized way, labeling problems, parts and expressions written down.

- ①  $3x_1 + 5x_2 + x_3 = 3$   
 $x_1 + 2x_2 + x_3 = 1$
- a) Write this system in the vector (matrix) form  $A\vec{x} = \vec{b}$ .
- b) Let  $B = [A, \vec{b}]$  be the augmented matrix. Show each step in the reduction of  $B$  to its "rref form"  $\text{rref}(B)$ .
- c) Write out the corresponding scalar equations, identifying the bound and free variables.
- d) Find the solution of the system.

- ②  $B = \begin{bmatrix} 0 & 1 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix}$
- a) If this is the rref form of the augmented matrix of a linear system, write out the corresponding equivalent scalar equations and identify bound and free variables.
- b) Find the solution of the system.