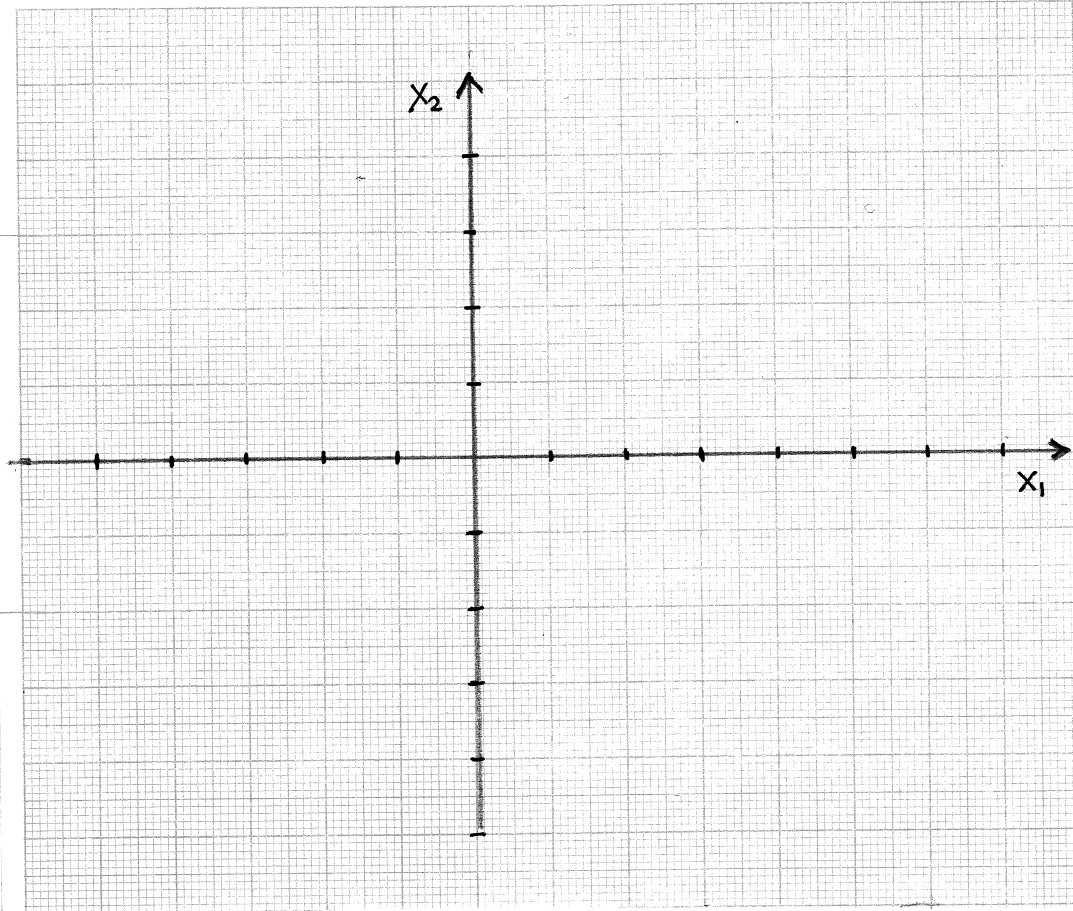


Lastname, Firstname:



old basis:

$$\vec{e}_1 = \langle 1, 0 \rangle \quad \vec{e}_2 = \langle 0, 1 \rangle$$

new basis:

$$\vec{b}_1 = \langle 1, 1 \rangle, \quad \vec{b}_2 = \langle -2, 1 \rangle$$

$$B = \langle \vec{b}_1 | \vec{b}_2 \rangle$$

$$= \begin{bmatrix} & \\ & \end{bmatrix}$$

basis changing matrix
(columns are new basis
vectors)

its inverse:

$$B^{-1} = \begin{bmatrix} & \\ & \end{bmatrix}$$

linear change of coordinates

$$\vec{x} \text{ in terms of } \vec{y}: \vec{x} = B\vec{y}$$

$$\vec{y} \text{ in terms of } \vec{x}: \vec{y} = B^{-1}\vec{x}$$

$$\text{matrix form: } \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \end{bmatrix}$$

$$\begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$\text{scalar form: } x_1 =$$

$$y_1 =$$

$$x_2 =$$

$$y_2 =$$

$$\text{point 1: } \langle x_1, x_2 \rangle = \langle -5, 1 \rangle \rightarrow \langle y_1, y_2 \rangle =$$

$$\text{point 2: } \langle y_1, y_2 \rangle = \langle 2, -1 \rangle \rightarrow \langle x_1, x_2 \rangle =$$

Instructions: Following the example handout, fill in the blanks above. Then reproduce the example graphic with \vec{e}_1, \vec{e}_2 then \vec{b}_1, \vec{b}_2 . Then use a ruler to create the new 4×4 grid of "unit parallelograms" formed with edges \vec{b}_1, \vec{b}_2 and their translated vectors as in the example. Draw in the y_1, y_2 axes on this grid and label them. Then graphically locate and draw in the position vectors of point 1 using the x -grid and point 2 using the y -grid. Confirm that the other coordinates you read off from the other grid agree with your computation above.