

Show all work, including mental steps, in a clearly organized way that speaks for itself. Use proper mathematical notation, identifying expressions by their proper symbols (introducing them if necessary), and use arrows and equal signs when appropriate. Always simplify expressions. **BOX** final short answers. **LABEL** parts of problem. Keep answers **EXACT** (but give decimal approximations for interpretation). Indicate where technology is used and what type (Maple, GC).

[You may use technology for row reductions, backsubstitutions and determinants although these may easily be done by hand.]

1. $v_1 = \langle 1, 0, 1, 0 \rangle$, $v_2 = \langle 0, 1, 0, 1 \rangle$, $v_3 = \langle 1, -1, 1, -1 \rangle$, $v_4 = \langle 1, 2, 1, 2 \rangle$,
 $v_5 = \langle 2, 1, 2, 1 \rangle$.

a) Express v_5 as a linear combination of the remaining 4 vectors. [Final answer: $v_5 = \dots$]

b) Check that this linear combination that you find actually evaluates to v_5 .

c) Find the independent linear relationships among these 4 vectors. Write out these relationships.

OPTIONAL. If you have time while others are finishing up, try this:

2. Demonstrate that the following vectors are linearly independent:

$u_1 = \langle 1, -1, 0, 0 \rangle$, $u_2 = \langle 1, 1, -1, -1 \rangle$, $u_3 = \langle 0, 0, 1, 1 \rangle$, $u_4 = \langle 1, -1, 1, -1 \rangle$.

► **solution**